

# Terahertz and High-Harmonic Radiation from Ultrafast Light Subgap or Above-Gap Driving of Spin-Orbit Proximitized Antiferromagnetic Mott Insulator

Federico Garcia-Gaitan<sup>1</sup>, Adrian E. Feiguin<sup>2</sup>, and Branislav K. Nikolić<sup>1,\*</sup>

<sup>1</sup>*Department of Physics and Astronomy, University of Delaware, Newark, Delaware 19716, USA*

<sup>2</sup>*Department of Physics, Northeastern University, Boston, Massachusetts 02115, USA*

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Ultrafast light-driven strongly correlated antiferromagnetic insulators, such as prototypical NiO with a large Mott energy gap  $\simeq 4$  eV, have recently attracted experimental attention using photons of both subgap [H. Qiu *et al.*, *Nat. Phys.* **17**, 388 (2021)] and above-gap energy [K. Gillmeister *et al.*, *Nat. Commun.* **11**, 4095 (2020)]. In the former context, which is also of great interest to applications, emission of terahertz (THz) radiation is observed from NiO/Pt bilayers, where heavy metal (HM) Pt introduces strong spin-orbit coupling (SOC) effects. However, in contrast to amply studied spintronic THz emitters using femtosecond laser pulse (fsLP)-driven FM/HM (where FM represents a ferromagnetic metal of the conventional type, such as Fe, Ni, or Co) bilayers, where ultrafast demagnetization takes place and is directly related to THz emission, microscopic mechanisms of electromagnetic (EM) radiation from NiO/HM bilayers remain obscure, as the total magnetization of NiO is zero before fsLP application. We employ the two-orbital Hubbard-Hund-Heisenberg model and study, via numerically exact quantum many-body methods, the dynamics of its Néel vector and nonequilibrium magnetization. This reveals *nonclassical* (i.e., not describable by the Landau-Lifshitz equation) dynamics of Néel vector and nonequilibrium magnetization, changing only in length while not rotating, where the former is substantially reduced in the case of above-gap fsLPs. Additionally, we compute EM radiation by time dependence of magnetization or of local charge currents, finding that both contributions are significant in the THz frequency range only in NiO with proximity SOC introduced by the HM layer. Outside the THz range, we find an integer high-harmonic generation, as well as unusual noninteger harmonics for the above-gap fsLP pump.

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**Introduction**—Pump-probe experiments [1] with strongly correlated antiferromagnetic (AFM) insulators (AFIs), such as prototypical NiO [2,3], have revealed [4] exotic effects interweaving nonequilibrium many-body physics and quantum coherence that can persist on surprisingly long time-scales (such as  $\sim 1$  ps [2,3]) due to a large Mott gap providing protection against fast thermalization and heating after photoexcitation. The femtosecond laser pulse (fsLP) in these experiments and typical theoretical studies [2,3,5] has a central frequency that is above the Mott gap between two Hubbard bands (Fig. 1). In the case of the subgap fsLP pump, theoretical interest has been focused [6–9] on understanding quantum tunneling, multiphoton absorption, and the so-called Keldysh crossover [10,11], as well as the ensuing nonlinear doublon-holon pair production. Such a panoply of complex nonequilibrium many-body states [4] cannot be found in fsLP-driven conventional band insulators and semiconductors governed by single particle quantum effects [12,13].

The same NiO material driven by subgap fsLPs, but in combination with a heavy metal (HM) layer (such as Pt, W,

or Ta) introducing effects [19] due to strong spin-orbit coupling (SOC), has very recently been explored [17,18] as a spintronic terahertz (THz) emitter [20–25]. Isolated

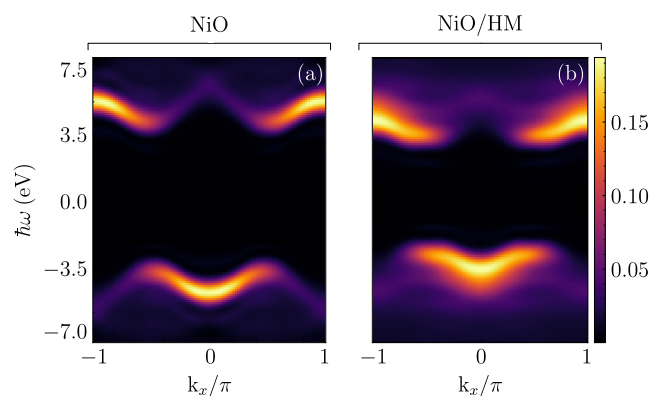


FIG. 1. The tDMRG-computed [14,15] spectral function [16] of the 2HHH model [2] on a ladder (Fig. 2) for (a) plain NiO and (b) NiO with proximity induced Rashba SOC due to an adjacent HM layer within a NiO/HM bilayer employed in THz spintronics experiments [17,18]. The upper and lower Hubbard bands separated by the Mott gap are clearly visible, where we focus on the bonding symmetry sector by choosing  $k_y = 0$  [15].

\*Contact author: bnikolic@udel.edu

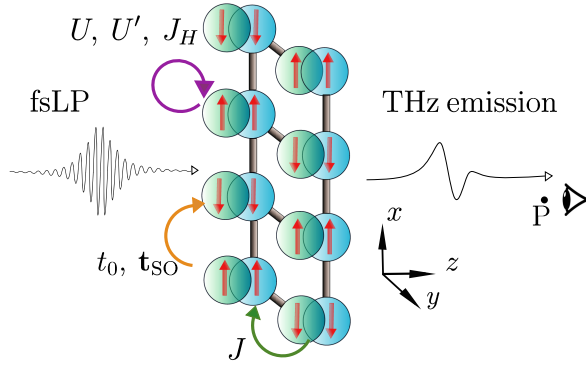


FIG. 2. Schematic view of two-orbitals-per-site 2HHH model [2] for NiO on  $4 \times 2$  ladder geometry. It can also include additional Rashba SOC [19,46], introduced through  $t_{SO}$  spin-dependent matrix hoppings [47], as arising from proximity effects [19,48–51] in NiO/HM bilayers employed experimentally [17,18]. Other denoted parameters describing local Coulomb and ( $U$  and  $U'$ ) Hund interactions ( $J_H$ ), Heisenberg exchange interactions ( $J$ ), and electron hopping ( $t_0$ ) between sites are explained in Eqs. (2)–(5). This setup is driven out of equilibrium by fsLPs, and we compute EM radiation emitted by it in both the THz and HHG frequency range.

ferromagnetic metal (FM) layers (such as Co, Fe, and Ni) or FM/HM bilayers have been intensely studied for nearly 30 years to understand ultrafast demagnetization [26,27], as well as THz emission by these systems. This emission is much stronger in the case of bilayers [20–24,28] than in the case of a single FM layer [23,28,29]. The fsLP in spintronic experiments typically has a central wavelength of  $\approx 800$  nm, so its photons have energy centered around  $\hbar\Omega_0 \approx 1.55$  eV, which is subgap [17,18,30] with respect to the Mott gap  $\approx 4$  eV of NiO (Fig. 1). The spintronic phenomena observed in such experiments have been interpreted [17,18] by borrowing the standard intuitive picture [20–24,28,31] (for its recent modifications, however, via microscopic theory, see Refs. [32–34]) developed for FM/HM bilayers. That is, an ultrafast spin current is somehow generated that flows from NiO into the HM layer such that the latter can convert it into charge current via the inverse spin Hall effect [35]. The time-dependent charge current is considered necessary to obtain sizable electromagnetic (EM) radiation in the far-field (FF) region (Fig. 2), as well as to interpret [17,18] the enhancement [23] of the emitted THz radiation when switching from FM to FM/HM systems. This is because magnetic dipole EM radiation [23,28,29] from time-dependent magnetization  $\mathbf{M}(t)$  is  $1/c$  smaller [32] than EM radiation by a time-dependent charge current, and magnetization of NiO induced out of equilibrium could be minuscule regardless. However, this picture does not explain the microscopic mechanism that generates the assumed spin current in NiO/HM bilayers (there is only speculation thus far [36]), or why the frequency spectrum of such current has features within the 0.1–3 THz range that are imprinted in the EM radiation

detected experimentally [17,18]. One can naively expect only that fsLPs will drive electrons into dynamics at its own center frequency  $\Omega_0$ , as well as at integer (typically odd [37,38]) multiples of  $\Omega_0$  for sufficiently intense fsLPs. Such high-harmonic generation (HHG) in current and EM radiation has been vigorously explored lately in diverse quantum materials [39,40], including strongly correlated ones [4,8,9,37,41,42]. Finally, it remains unclear what type of dynamics is obeyed by the Néel vector (as the difference of magnetizations of two sublattices) and magnetization [as the sum of sublattice magnetizations, which is necessarily a nonequilibrium quantity because  $\mathbf{M}(t=0) \equiv 0$ ] when compared to standard demagnetization [23,26,27] of a FM layer whose magnetization vector shrinks. In the case of thin FM layers, a rapid and straightforward analysis of the direction of  $\mathbf{M}(t)$  and its magnitude is achieved via magneto-optical Kerr or Faraday effects [23]. In contrast, they do not apply to AFIs, so novel ideas have been explored [43] to detect the presumed rotation of their Néel vector [18,44,45].

Thus, developing a microscopic understanding of the response of AFIs to subgap fsLPs (that is, by starting with a suitable quantum many-body Hamiltonian and using tools of nonequilibrium quantum statistical mechanics) would also help to resolve a number of outstanding issues in AFM optospintronics [52]. Note that, specifically for NiO, which is a strongly correlated material sharing properties of both Mott and charge-transfer insulators [2,3,53], x-ray techniques applied as a probe after a subgap fsLP pump have revealed [30] possible substantial changes of its electronic structure [1,5], such as the emergence of midgap states and Hubbard gap reduction persisting on timescales greater than 2 ps. Such phenomena originating from charge dynamics must be considered together with local spin dynamics, as they can lead to inextricable complex spin-charge dynamics [2,3,54]. In the case of weakly correlated FMs, a proper microscopic description of spin-charge dynamics is achieved via time-dependent density functional theory (TDDFT), which has provided [55–59] a most detailed insight into a sequence of fast-changing events [60] and their effect [31–33] on THz emission. However, applications [61] of TDDFT to NiO are impeded by intricacies including a time-dependent [4,62,63] Hubbard  $U$  [64] to properly capture a strong on-site Coulomb interaction that is also dynamical (as opposed to a static  $U$  in well-developed conventional equilibrium DFT +  $U$  calculations [67], where DFT stands for density functional theory).

In this Letter, we aim to capture all the essential physics of strongly correlated electrons within NiO in the presence of fsLPs and SOC by employing a two-orbital Hubbard-Hund-Heisenberg (2HHH) model [2] and by simulating its time evolution via numerically exact quantum many-body methods. Its ground AFM state is formed by local spins  $S = 1$  [68] at each site that are composed of two elemental spins  $s = 1/2$  located on two orbitals at that site (Fig. 2),

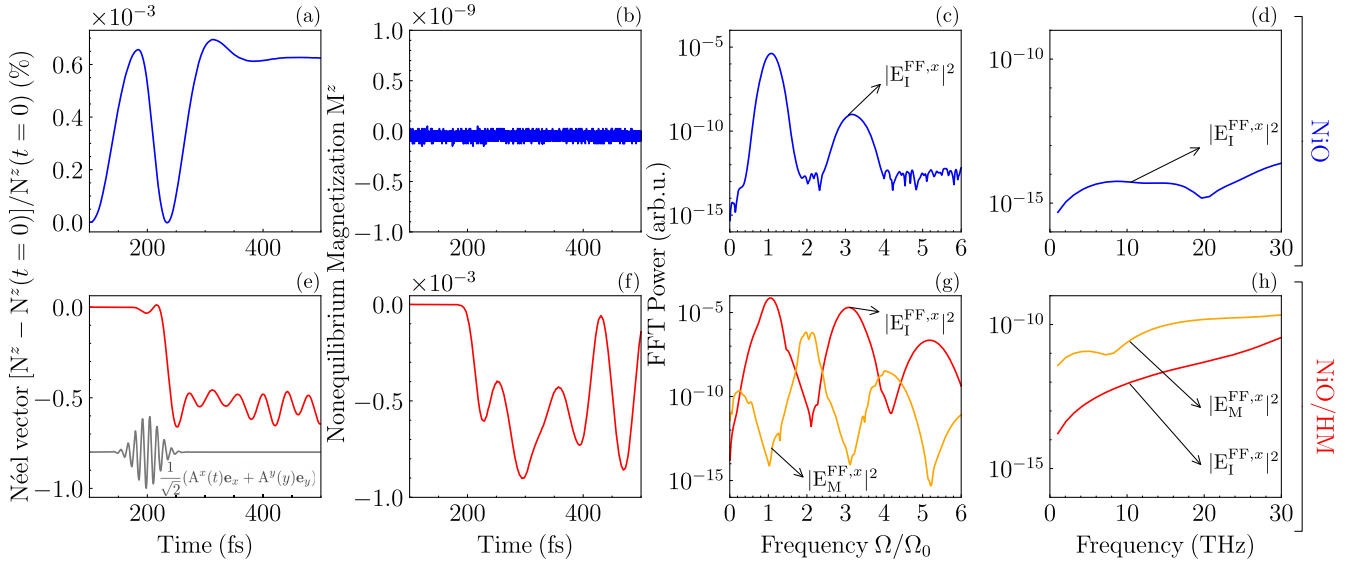


FIG. 3. Time dependence, initiated by a fsLP with subgap central frequency, of (a),(e) the Néel vector and (b),(f) nonequilibrium magnetization. (c),(d),(g),(h) Fast Fourier transform (FFT) power spectrum—within (c),(g) HHG frequencies or (d),(h) THz frequencies—of the x component of the electric field of EM radiation emitted by the dynamics of magnetization [Eq. (A3)] or bond charge currents [Eq. (A2)]. Top row: plain NiO. Bottom row: NiO assumed to contain [19] the Rashba SOC due to proximity effects [48–51] from the HM layer within the NiO/HM bilayer studied in recent experiments [17,18].

with Hund interaction included between them to achieve a fixed and stable  $S$  per atom [69,70]. In addition, to consider the adjacent nonmagnetic HM layer in THz spintronics experiments [17,18], we also include SOC of the Rashba type [19,46] in the 2HHH model of Ref. [2]. Thereby introduced SOC models proximity effects [19,48–51] around the NiO/HM interface, which modify the electronic structure on the NiO side due to the HM layer (NiO, in turn, modifies bands of the HM layer, but we do not model the HM layer explicitly due to high computational expense [71]). This model is placed onto a ladder geometry (Fig. 2), allowing for its spectral function (Fig. 1) to be computed [14–16] via numerically (quasi)exact simulations using time-dependent density matrix renormalization group (tDMRG) methods [72–75] applicable to quasi-one-dimensional (quasi-1D) lattices. We complement the study with an additional set of numerical simulations using massively parallel exact diagonalization (ED) methods [76] for Hubbard-type systems, implemented within the HΦ package [77,78]. This technique allows us to access longer times (required for THz radiation calculations) than those possible via tensor network algorithms (like tDMRG) encountering the “entanglement barrier” [79,80]. Our principal results, revealing highly nonclassical dynamics of Néel vector and nonequilibrium magnetization, and the ensuing EM radiation at both HHG of fsLP and in a much lower THz range are given in Figs. 3 and 4. Before discussing these results, we introduce useful concepts and notations.

**Model and methods**—The monolayer [71] of NiO is modeled on a tight-binding ladder (Fig. 2) with two orbitals

per site hosting Ni only, while the O atom is not modeled explicitly, albeit O-mediated interactions are included. The same 2HHH model, but without any SOC, was used in Ref. [2], where above-gap pumping of NiO by fsLP was studied experimentally and theoretically. Our Hamiltonian,

$$\hat{H}_{2HHH} = \hat{H}_{\text{local}} + \hat{H}_{\text{ex}} + \hat{H}_{\text{TB}} + \hat{H}_{\text{SOC}}, \quad (1)$$

is built on top of the model from Ref. [2] by including proximity induced Rashba SOC [19,46] to describe the NiO/HM bilayer used in THz spintronics experiments [17,18]. The local terms of  $\hat{H}_{\text{local}}$  account for the Hubbard and Hund physics

$$\begin{aligned} \hat{H}_{\text{local}} = & U \sum_{i,\alpha} \hat{n}_{i,\alpha\uparrow} \hat{n}_{i,\alpha\downarrow} - \mu \sum_{i,\alpha,\sigma} \hat{n}_{i\alpha\sigma} - g\mu_B B_z^{\text{imp}} \hat{s}_{1\alpha}^z \\ & + \sum_{i,\alpha < \beta} \sum_{\sigma,\sigma'} (U' - J_H \delta_{\sigma\sigma'}) \hat{n}_{i\alpha\sigma} \hat{n}_{i\beta\sigma'} \\ & + \gamma J_H \sum_{i,\alpha \neq \beta} (\hat{c}_{i\alpha\uparrow}^\dagger \hat{c}_{i\alpha\downarrow}^\dagger \hat{c}_{i\beta\downarrow} \hat{c}_{i\beta\uparrow} + \text{H.c.}) \\ & + \gamma J_H \sum_{i,\alpha \neq \beta} (\hat{c}_{i\alpha\uparrow}^\dagger \hat{c}_{i\beta\downarrow}^\dagger \hat{c}_{i\alpha\downarrow} \hat{c}_{i\beta\uparrow} + \text{H.c.}). \end{aligned} \quad (2)$$

Here  $\hat{c}_{i\alpha\sigma}$  ( $\hat{c}_{i\alpha\sigma}^\dagger$ ) is the creation (annihilation) operator of an electron of spin  $\sigma = \uparrow, \downarrow$  in orbital  $\alpha = 1, 2$  located at site  $i$ ;  $\hat{n}_{i\alpha\sigma}$  is the corresponding number operator;  $U$ ,  $U'$ , and  $J_H$  are the intraorbital Coulomb, interorbital Coulomb, and interorbital (or Hund [69,70]) exchange interaction, respectively;  $\mu$  is the on-site chemical potential; and  $B_z^{\text{imp}}$  is a

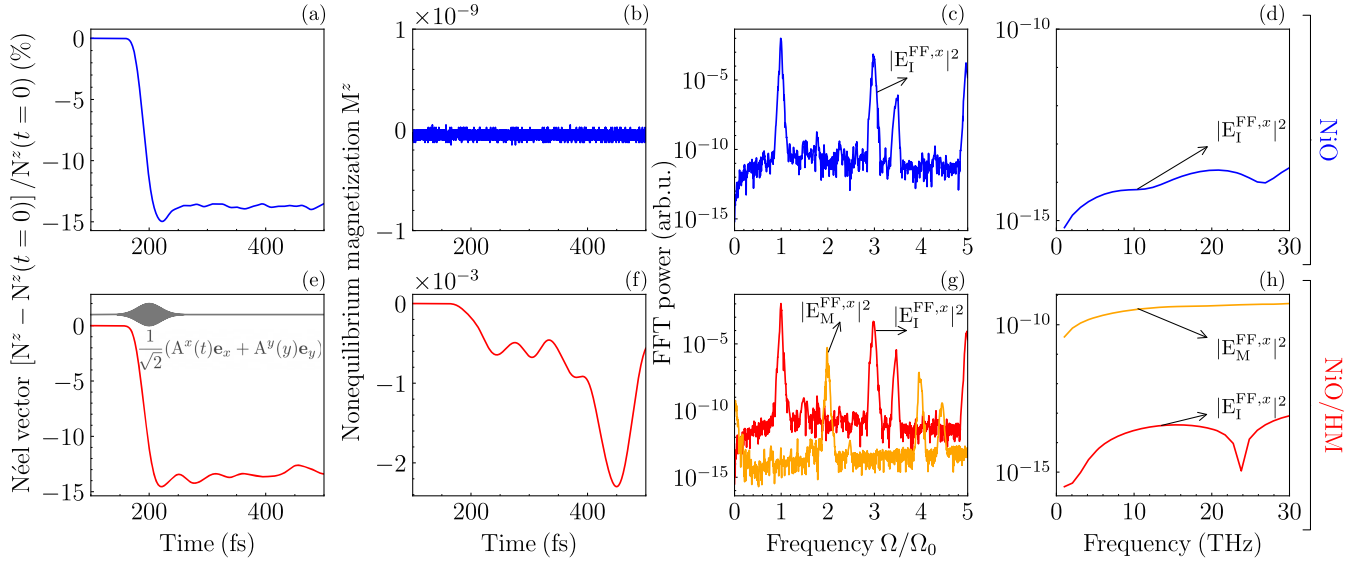


FIG. 4. The same information as in Fig. 3 but using fsLP, whose central frequency of  $\hbar\Omega_0 = 8$  eV is above gap in relation to Fig. 1.

magnetic field added [81] on site  $i = 1$  to lift the degeneracy between spin-up and spin-down electrons. The Heisenberg exchange interaction between spins at nearest neighbor (NN) sites is given by

$$\hat{H}_{\text{ex}} = \sum_{\langle ij \rangle, \alpha} [J(\hat{s}_{i\alpha}^x \cdot \hat{s}_{j\alpha}^x + \hat{s}_{i\alpha}^y \cdot \hat{s}_{j\alpha}^y) + J_z \hat{s}_{i\alpha}^z \cdot \hat{s}_{j\alpha}^z], \quad (3)$$

where  $\langle ij \rangle$  denotes summation over the NN sites;  $\hat{s}_{i\alpha}^p = \sum_{\sigma, \sigma'} \hat{c}_{i\alpha\sigma}^\dagger \frac{1}{2} \hat{\sigma}_{\sigma\sigma'}^p \hat{c}_{i\alpha\sigma'}$  is the electron spin operator expressed using  $\hat{\sigma}^p$  as one of three ( $p = x, y, z$ ) Pauli matrices; and  $J = J_z = 0.1$  eV in the isotropic case. The tight-binding (TB) Hamiltonian

$$\hat{H}_{\text{TB}} = -t_0 \sum_{\langle ij \rangle, \alpha, \sigma} (\hat{c}_{i\alpha\sigma}^\dagger \hat{c}_{j\alpha\sigma} + \text{H.c.}), \quad (4)$$

serves as the kinetic term, where  $t_0$  is the hopping parameter. An additional TB term

$$\hat{H}_{\text{SOC}} = \sum_{\langle ij \rangle, \alpha} (\hat{\mathbf{c}}_{i\alpha}^\dagger \mathbf{t}_{\text{SO}} \hat{\mathbf{c}}_{j\alpha} + \text{H.c.}) \quad (5)$$

is employed to introduce proximity SOC—switched off in the NiO case and switched on in the NiO/HM case in Figs. 3 and 4. Here  $\hat{\mathbf{c}}_{i\alpha}^\dagger = (\hat{c}_{i\alpha\uparrow}^\dagger \hat{c}_{i\alpha\downarrow}^\dagger)$  denotes the row vector of two creation operators and  $\mathbf{t}_{\text{SO}}$  is a direction-dependent  $2 \times 2$  matrix hopping [47] with values  $-it_{\text{SO}}\hat{\sigma}_y$  ( $it_{\text{SO}}\hat{\sigma}_x$ ) for horizontal (vertical) bonds, where we use  $t_{\text{SO}} = 0.5$  eV. The  $\hat{H}_{\text{SOC}}$  term is of the Rashba type [46], assumed to originate from proximity to the HM layer employed experimentally [17,18], as found in conventional equilibrium DFT calculations on FM/HM [19] of AFI/HM [50] bilayers [71]. Realistic parameter values for NiO are taken from prior first-principles calculations for strongly

correlated electrons [82], such as from DFT +  $U$  [67] and/or DFT plus dynamical mean field theory [83,84] studies:  $U \approx 8$  eV,  $t_0 \approx 1$  eV, and  $J_H \approx 1$  eV; we set  $U' = U - 2J_H$  and  $\gamma = 1$  for symmetry reasons [85]. Half filling is selected by setting the chemical potential to  $\mu = (3U - 5J_H)/2$  [2]. The magnetic field at site 1,  $g\mu_B B_z^{\text{imp}} = 0.1$  eV, as generated by, e.g., a static impurity, induces [81] Néel “checkerboard” order  $\langle \hat{S}_i^z \rangle = -\langle \hat{S}_j^z \rangle \neq 0$  ( $i$  and  $j$  are two NN sites) in the ground state (GS). Nevertheless, the GS in our simulations retains nonzero entanglement, as witnessed in many recent experiments even at finite temperature [86,87], so it is not identical to an unentangled Néel ket  $|\uparrow\downarrow \cdots \uparrow\downarrow\rangle$ .

The fsLP is introduced via its vector potential [the gray line in Figs. 3(e) and 4(e)] of amplitude  $A_{\text{max}}$ , which couples to electrons in the form of a Peierls phase [88,89] multiplying hoppings in Eqs. (4) and (5) by a factor  $P = \exp[iz_{\text{max}} e^{-(t-t_p)^2/2\sigma_{\text{light}}^2} \cos(\Omega_0 t)]$ , so  $t_0(t) = Pt_0$  and  $\mathbf{t}_{\text{SO}}(t) = P\mathbf{t}_{\text{SO}}$  [90]. Here  $z_{\text{max}} = ea_0 A_{\text{max}}/\hbar = 0.2$  is the dimensionless parameter [12] quantifying the fsLP intensity,  $a_0$  is the lattice constant, and  $\sigma_{\text{light}} = 20$  fs determines the width of the Gaussian envelope, which is initially centered at  $t_p = 200$  fs. The center frequency of the fsLP is either  $\hbar\Omega_0 = 1.55$  eV in Fig. 3, corresponding to a subgap 800 nm wavelength commonly employed in THz spintronic experiments [17,18,20–24,28], or  $\hbar\Omega_0 = 8$  eV in Fig. 4 for above-gap fsLP (gaps are shown in Fig. 1). The electric field of the fsLP is linearly polarized along the  $x - y$  direction (i.e., diagonal to the ladder) in Fig. 2. The time evolution described by  $\hat{H}(t)$  on a  $4 \times 2$  ladder [92] is computed via massively parallel ED [76] using the HΦ package [77,78], where the GS was found using the Lanczos algorithm and the evolution operator is computed via a Taylor expansion



considering up to 15 terms. The time step was chosen as  $\delta t = 0.005\hbar/t_0$ .

Time-dependent magnetization  $M^z(t)$  and Néel vector  $N^z(t)$  are obtained by summing spin expectation values at each site,  $M^z = \sum_i M_i^z = \sum_{i,a} \langle \hat{s}_{ia}^z \rangle(t)$  and  $N^z = \sum_i N_i^z = \sum_{i,a} (-1)^i \langle \hat{s}_{ia}^z \rangle(t)$ , where a “snakelike” enumeration of ladder sites is assumed. Note that other components (the  $x$  and  $y$  components) are vanishingly small. Our methodology for computing EM radiation, due to time-dependence of bond charge currents  $I_{ij}$  or the  $z$ -component of nonequilibrium magnetization  $M^z$ , is explained in the End Matter.

**Results and discussion**—The usual first take at interpreting experiments on subgap light-driven AFIs, including NiO [18,101,102], invokes [101–104], a direct coupling of the light magnetic field (or an effective one due to inverse Faraday [102] or inverse Cotton-Mouton [18] effects) to local magnetization of AFIs. This leads to classical dynamics of the Néel vector, which rotates without changing its length [18], in accord with phenomenological theories [44,45] of the Landau-Lifshitz (LL) type [105]. However, limitations of this approach are often found in experiments [102,106], which is not surprising, as light-charge coupling is much stronger [56], so electrons should be explicitly included. But the picture of classical LL dynamics [18,44,45] is appealing because it is difficult to develop intuition on how electrons of AFIs, with a gapped energy spectrum (Fig. 1), absorb subgap light and then affect its magnetic ordering. In the case of AFM metals, it is easy to envisage (and calculate [93]) that fsLP generates a photocurrent of conduction electrons, which are then spin polarized by the magnetic background and exert spin torque [93] onto local magnetization. Its dynamics follow (for weak-intensity fsLP to avoid demagnetization [26,27]) classical LL dynamics. Note that such dynamics can be justified only for AFs whose localized spins are  $S > 1$  and for sufficiently high temperatures of their dissipative environment [107].

For AFIs, where the Hubbard interaction is much stronger than in the metallic case, there is no such shortcut, and one has to handle the complexities of the photoexcited Hubbard model [4–9,108]. In addition, because NiO hosts localized spins  $S = 1$ , we can anticipate [107] their non-classical (i.e., outside of any description by LL-type theories [18,44]) dynamics. Indeed, our quantum many-body calculations for subgap fsLP-driven NiO reveal highly non-classical [81,109,110] dynamics of the Néel vector and magnetization in Fig. 3. That is, both vectors are changing length along the  $z$  axis (orthogonal to the ladder in Fig. 2) while not rotating at all. Nonequilibrium magnetization remains zero in plain NiO [Fig. 3(b)]. However,  $M^z(t) \neq 0$  in SO proximitized NiO [Fig. 3(f)], which is akin to experimentally observed [111] weak ferromagnetism in a photodoped Mott insulator with native SOC. The nonzero  $\partial_t M^z(t_r)$  emits magnetic dipole [Eq. (A3)] THz radiation

[the orange line in Fig. 3(h)], which can (surprisingly, when compared to FM/HM bilayers [32]) surpass the contribution from  $\partial_t I_{ij}(t_r)$  [the red curve in Fig. 3(h)]. Importantly, THz emission from both of these two sources is significant only when proximity SOC is present in NiO/HM bilayer [Fig. 3(h)], in full accord with experiments [17,18]. Thus, our theory explains these experiments without invoking qualitative speculations [17,18,36], while showing that concepts borrowed from FM/HM systems (like interlayer spin current and spin-to-charge conversion within HMs [20,21,23,24,28,33]) are not necessary for THz emission from an AFI. The magnetic dipole EM radiation exhibits even integer HHG [Fig. 3(g)], while odd ones are expected [37] for radiation from  $\partial_t I_{ij}(t_r)$ , as dictated by symmetry-imposed selection rules of Floquet group theory [112]. Although SOC breaks inversion symmetry, odd integer HHG is preserved [38,113]. This offers a scheme—detect even HHG in EM radiation from an AFI—which directly corroborates how magnetization dynamics in magnets driven by fsLP can be much faster [58,114] than observed in low-energy transport experiments [36].

For above-gap fsLP in Fig. 4, we find reduction of Néel vector by up to 15%, signifying suppression [5] of AFM order in the GS. This is in sharp contrast to its minuscule change for subgap fsLP in Fig. 3. As with subgap fsLPs, nonequilibrium magnetization [compare Figs. 4(f) and 4(b)] emerges only when proximity SOC is switched on. Unlike the subgap fsLP case, the charge current and its THz radiation are not significantly enhanced by including proximity SOC [Fig. 4(d) vs Fig. 4(h)]. The selection rules for HHG remain the same, allowing only odd integer HHG of  $E_I^{\text{FF},x}$  [Figs. 4(c) and 4(g)] and even ones of  $E_M^{\text{FF},x}$  [Fig. 4(g)]. Curiously, we also find noninteger HHG [Figs. 4(c) and 4(g)] of both  $E_I^{\text{FF},x}$  and  $E_M^{\text{FF},x}$ , which are beyond standard Floquet theory and its selection rules [112]. Theoretical [37,96] and experimental reports [40] of noninteger HHG are scarce [4], and their understanding is in its infancy. For example, they could arise [37] from a correlation-driven population of multiple Floquet states (unlike the population of a single state used in Floquet group theory [112]), whose exploration we relegate to future studies [115].

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**Data availability**—The data that support the findings of this Letter are not publicly available upon publication

because it is not technically feasible and/or the cost of preparing, depositing, and hosting the data would be prohibitive within the terms of this research project. The data are available from the authors upon reasonable request.

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## End Matter

To compute EM radiation generated by the charge dynamics, the expectation value  $I_{ij} \equiv \langle \hat{I}_{ij} \rangle$  of the bond charge current operator [47],

$$\hat{I}_{ij} = \frac{ie}{\hbar} \sum_{\alpha} [\hat{\mathbf{c}}_{i\alpha}^{\dagger} \{t_0(t) \hat{\sigma}_0 + \mathbf{t}_{\text{SO}}(t)\} \hat{\mathbf{c}}_{j\alpha} - \text{H.c.}], \quad (\text{A1})$$

from site  $i$  to site  $j$ , with  $\hat{\sigma}_0$  being a unit  $2 \times 2$  matrix, is plugged into [34,93,116] the Jefimenko formula [117] for the electric field,

$$\mathbf{E}_I^{\text{FF}}(\mathbf{r}, t) = \frac{1}{4\pi\epsilon_0 c^2} \sum_{P_{i \rightarrow j}=1}^{N_b} \int_{P_{i \rightarrow j}} \left[ (\mathbf{r} - \mathbf{l}) \frac{\partial_t I_{ij}(t_r)}{|\mathbf{r} - \mathbf{l}|^3} (\mathbf{r} - \mathbf{l}) \cdot \mathbf{e}_x - \frac{\partial_t I_{ij}(t_r)}{|\mathbf{r} - \mathbf{l}|} \mathbf{e}_x \right] dl. \quad (\text{A2})$$

The most general Jefimenko formula [117], as the proper solution of the Maxwell equations [118], is reorganized [119] above to isolate the FF contributions decaying as  $\sim 1/r$ . Note that the Jefimenko equation (A2) can also be

viewed [118] as the proper (i.e., time-retarded) time-dependent generalizations of the Coulomb law. Here  $t_r \equiv t - |\mathbf{r} - \mathbf{l}|/c$  emphasizes retardation in the response time due to relativistic causality [117,119]. Additionally, we adapt [93,116] Eq. (A2) to utilize the expectation value of time-dependent bond charge currents [Eq. (A1)] as the source of EM radiation—they are the counterpart on the TB lattice of the local current density in continuous space. Such bond currents are assumed to be homogeneous [34,93,116] along the path  $P_{i \rightarrow j}$  from site  $i$  to site  $j$  of length  $dl$ ,  $N_b$  is the number of bonds, and we use the shorthand notation  $\partial_t \equiv \partial/\partial t$ . Finally, we also compute the magnetic dipole contribution to FF radiation, as generated by the time dependence of the nonequilibrium magnetization,

$$\mathbf{E}_M^{\text{FF}}(\mathbf{r}, t) = \frac{1}{4\pi\epsilon_0 c^3} \sum_i \frac{\mathbf{r} - \mathbf{l}_i}{|\mathbf{r} - \mathbf{l}_i|^2} \times \partial_t^2 \mathbf{M}_i(t_r), \quad (\text{A3})$$

where  $\mathbf{l}_i$  indicates the location of the site  $i$ . Both contributions to EM radiation are computed at point  $P$  in Fig. 2, which is  $100a_0$  away from NiO.

# Supplemental Material for “Terahertz and High-Harmonic Radiation from Ultrafast Light Subgap or Above-Gap Driving of Spin-Orbit Proximitized Antiferromagnetic Mott Insulator”

Federico Garcia-Gaitan,<sup>1</sup> Adrian E. Feiguin,<sup>2</sup> and Branislav K. Nikolić<sup>1,\*</sup>

<sup>1</sup>*Department of Physics and Astronomy, University of Delaware, Newark DE 19716, USA*

<sup>2</sup>*Department of Physics, Northeastern University, Boston, MA 02115, USA*

This Supplemental Material provides one additional Fig. S1 examining the efficiency of electron-spin interaction as a dissipation channel, where energy is transferred from the electrons to the spins. This channel is opened by our quasi-one-dimensional ladder geometry [1] (even faster relaxation by the same channel occurs in two-dimensional geometry [2]), as well as the presence of more than one orbital per its site [3]. That is, in dimensions greater than one, where spin-charge separation [4] characterizing 1D Mott insulators [4] is suppressed, an electron moving through an antiferromagnetically (AFM) ordered background flips a spin in every hopping process [2]. This process then leads to an intrinsically strong spin-charge interaction, that can be relevant even in the paramagnetic phase where spin correlations are short-ranged and short-lived [1].

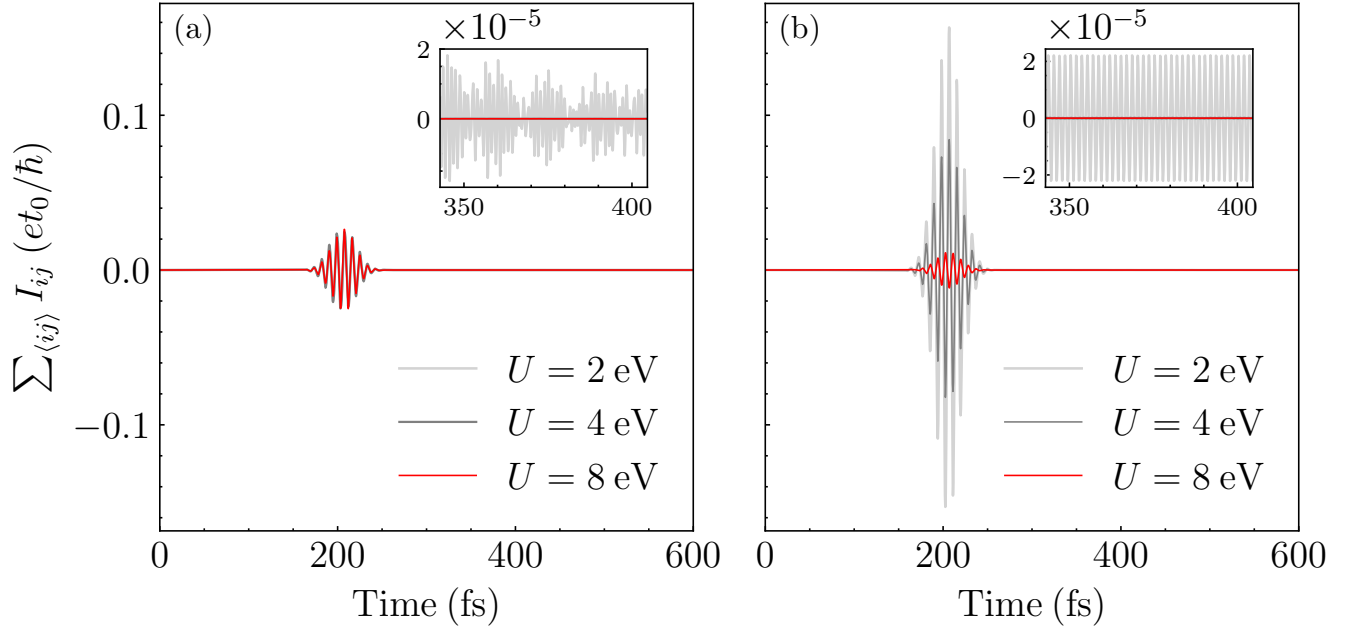


FIG. S1. Time dependence of the sum (over all pairs of nearest-neighbor sites, as denoted by  $\langle ij \rangle$ ) of all bond charge currents [i.e., expectation values of bond current operator in Eq. (A1) of the main text] for: (a) fsLP-driven 2HHH model of NiO [Eq. (1) in the main text, but without proximity spin-orbit coupling term,  $\hat{H}_{\text{SOC}} = 0$ ], using different values of Hubbard  $U$  at fixed Hund coupling  $J_H = 1$  eV; and (b) fsLP-driven plain Hubbard model with a single orbital per site on an identical ladder geometry. The central frequency of fsLP is subgap when compared to the Mott gap (Fig. 2 in the main text) opened by  $U = 8$  eV.

Figure S1(a) confirms that the sum of all bond charge currents  $\sum_{\langle ij \rangle} I_{ij}$  decays with increasing on-site Coulomb interaction (determined by Hubbard  $U$ ). This is because as  $U$  increases, the system undergoes a phase transition from a metallic phase to a Mott insulating phase (note that we use  $U = 8$  eV in the main text) favoring magnetic ordering, thereby enabling *dissipation of electron energy into bosonic excitations of AFM ordered background* [1, 2, 5]. Such current relaxation occurs despite the *absence* of phonons (as the other possible source of bosonic bath [6], but dissipating electron energy over much longer time scales [7]) in our calculations. We note that phonons are

\* bnikolic@udel.edu



considered necessary [7] to relax femtosecond laser pulse (fsLP)-driven weakly correlated magnets and bring their charge photocurrents to zero [6]. Thus, we conclude that short-range spin correlations act as an efficient dissipative environment for mobile charge carriers in our two-orbital Hubbard-Hund-Heisenberg (2HHH) model [2, 5] of NiO. To understand the effect of its many orbitals per site, we also provide in Fig. S1(b) the result of the same calculations for the plain Hubbard model with a single orbital per site. By comparing Fig. S1(a) with Fig. S1(b) we learn that electron-spin dissipation channel associated with Hund coupling  $J_H$  (i.e., many orbitals per site) dominates at early times. On the other hand, the Hubbard  $U$  mediated dissipation mechanism becomes more relevant at longer times—this is clarified by the insets of both panels in Fig. S1 where current oscillations are suppressed, noticeably at later times, as  $U$  is increasing.

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